FIRST SEMESTER (CUFYUGP) DEGREE EXAMINATION NOVEMBER 2024

Computer Application

BCA 1CJ 102—MATHEMATICAL FOUNDATION FOR COMPUTER APPLICATIONS

(2024 Admission onwards)

Time: Two Hours

Maximum Marks: 70

Section A

Answer all questions.

Each question carries 3 marks.

(Ceiling 24 marks)

- 1. Define rank of a matrix. What is the rank of $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$?
- 2. Write a short note on cofactors and minors.

3. If
$$A = \begin{bmatrix} 2 & 3 \\ 1 & 2 \end{bmatrix}$$
 and $B = \begin{bmatrix} 4 & 2 \\ 1 & 3 \end{bmatrix}$. Find $6A - 3B$.

- 4. What is a characteristic vector?
- 5. Explain non-homogeneous system of linear equations.
- 6. Find $a \cdot b$ when $a = \langle 2, 2, -1 \rangle$ and $b = \langle 5, -3, 2 \rangle$.
- 7. State mean value theorem.
- 8. Define quotient rule.
- 9. Find the antiderivative of the function $3x^2 + 4x^3$.
- 10. Evaluate $\int (2x^2 + e^x) dx$.

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Section B

Answer all questions.

Each question carries 6 marks.

(Ceiling 36 marks)

- 11. Write a short note on operations on matrices.
- 12. What are the elementary transformations of matrices?
- 13. Solve the system of linear equations by Gauss Siedel method:

$$2x + y = 8$$
$$x + 2y = 1$$

- 14. Find the eigenvalues of the matrix $\begin{bmatrix} -2 & -4 & 2 \\ -2 & 1 & 2 \\ 4 & 2 & 5 \end{bmatrix}$.
- 15. Briefly explain different types of vectors.
- 16. Differentiate $\frac{x^3 + 2x}{x 1}$.
- 17. Explain: Indefinite integral and constant of integration.
- 18. Find $\int \sin(x^3) \cdot 3x^2$.

Section C

Answer any **one** question. The question carries 10 marks.

19. Find the inverse of the matrix
$$\begin{bmatrix} 3 & 5 & 7 \\ 2 & -3 & 1 \\ 1 & 1 & 2 \end{bmatrix}$$

20. Find
$$\frac{dy}{dx}$$
 if $y = \frac{4\sin x}{2x + \cos x}$.

 $(1 \times 10 = 10 \text{ marks})$